

Trinity College

Semester Two Examination, 2017

Question/Answer booklet

MATHEMATICS SPECIALIST UNITS 1 AND 2 Section One: Calculator-free		If required by your examination administrator, please place your student identification label in this box		
Student Number:	In figures			
	In words			
	Your name			
Time allowed for this s	section			

Reading time before commencing work: Working time:

five minutes fifty minutes

Materials required/recommended for this section

To be provided by the supervisor This Question/Answer booklet Formula sheet

To be provided by the candidate

Standard items: pens (blue/black preferred), pencils (including coloured), sharpener, correction fluid/tape, eraser, ruler, highlighters

Special items: nil

Important note to candidates

No other items may be taken into the examination room. It is **your** responsibility to ensure that you do not have any unauthorised material. If you have any unauthorised material with you, hand it to the supervisor **before** reading any further.

Structure of this paper

Section	Number of questions available	Number of questions to be answered	Working time (minutes)	Marks available	Percentage of examination
Section One: Calculator-free	8	8	50	52	35
Section Two: Calculator-assumed	13	13	100	99	65
				Total	100

Instructions to candidates

- 1. The rules for the conduct of Trinity College examinations are detailed in the *Instructions to Candidates* distributed to students prior to the examinations. Sitting this examination implies that you agree to abide by these rules.
- 2. Write your answers in this Question/Answer booklet.
- 3. You must be careful to confine your response to the specific question asked and to follow any instructions that are specified to a particular question.
- 4. Additional working space pages at the end of this Question/Answer booklet are for planning or continuing an answer. If you use these pages, indicate at the original answer, the page number it is planned/continued on and write the question number being planned/continued on the additional working space page.
- 5. Show all your working clearly. Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat any question, ensure that you cancel the answer you do not wish to have marked.
- 6. It is recommended that you do not use pencil, except in diagrams.
- 7. The Formula sheet is not to be handed in with your Question/Answer booklet.

TRINITY COLLEGE CALCULATOR-FREE

SEMESTER 2 2017 SPECIALIST UNITS 1 AND 2

Section One: Calculator-free

This section has **eight (8)** questions. Answer **all** questions. Write your answers in the spaces provided.

Working time: 50 minutes.

Question 1

(6 marks)

35% (52 Marks)

(a) Solve the real quadratic equation $z^2 - 4z + 8 = 0$. Express the answer in simplest form. (3 marks)

(b) Determine the values of the real constants *b* and *c* if z = 1 + 3i is a solution of the equation $z^2 + bz + c = 0$. (3 marks)

Question 2

(6 marks)

(a) A set of real numbers is given by $\{\sqrt{2}, 3.\overline{14}, \pi, \sqrt[3]{14}\}$. Clearly show that one of the numbers in the set is rational. (3 marks)

(b) Show that if *n* is one more than a multiple of three, then n^2 will also be one more than a multiple of three, where $n \in \mathbb{Z}$. (3 marks)

TRINITY COLLEGE CALCULATOR-FREE

Question 3

The complex numbers u and v are shown in the complex plane below.



Plot and label the following complex numbers:

(a)
$$z_1 = u + v.$$
 (1 mark)

(b)
$$z_3 = \bar{v}$$
.

(c) $z_4 = \overline{u+v} - \overline{u} - \overline{v}$. (2 mark)

5

(4 marks)

(1 mark)

(8 marks)

Question 4

Relative to the origin *O*, the points *A*, *B* and *C* have position vectors $\mathbf{a} = 5\mathbf{i} - 6\mathbf{j}$, $\mathbf{b} = \mathbf{i} - 3\mathbf{j}$ and $\mathbf{c} = -8\mathbf{i} + 15\mathbf{j}$ respectively.

(a) Determine in Cartesian form

(i) the vector
$$\overrightarrow{AB}$$
. (1 mark)

(ii) a vector **d**, parallel to \overrightarrow{AB} and of magnitude $\sqrt{5}$. (3 marks)

(b) If $\mathbf{c} = \lambda \mathbf{a} + \mu \mathbf{b}$, determine the values of the constants λ and μ . (4 marks)

TRINITY COLLEGE CALCULATOR-FREE			7	SE SPECIALIS	
Quest	ion 5	i			
Let A =	= [⁸ 5	$\begin{bmatrix} 3\\2 \end{bmatrix}$ and $B = \begin{bmatrix} 2 & 4\\ -3 & -1 \end{bmatrix}$.			
(a)	Dete	ermine			
	(i)	3A-B.			

(2 marks) (ii) BA.

(iii) A^{-1} . (2 marks)

Use a matrix method to solve the system of equations 8x + 3y = 10 and 5x + 2y = 7. (3 marks) (b)

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(9 marks)

(2 marks)

(i) $\cos \theta = \sin 38^{\circ}$. (2 marks)

(ii) $\sec \theta = \csc 100^{\circ}$.

(2 marks)

(8 marks)

(b) Prove that $\tan x + \sec x = \frac{\cos x}{1 - \sin x}$.

(4 marks)

Question 7

Cyclic quadrilateral *ABCD* has diagonals *AC* and *BD* that intersect at *M*. Given that AM = 6 cm, CM = 8 cm and BD = 16 cm, determine the smallest possible length of *BM*.

9

(5 marks)

Question 8

(6 marks)

Let z_1 and z_2 be complex numbers such that $2z_1 + 3z_2 = 7$ and $z_1 + iz_2 = 4 + 4i$.

Determine z_1 and z_2 in the form z = a + bi, where $a, b \in \mathbb{Z}$.

Additional working space

Question number: _____